

All collisions + explosions

Momentum

$$\sum P_i = \sum P_f$$

$$m_c v_c + 0 = m_c y + m_b x$$

$$0.220 \times 44 = 0.220 y + 0.046 x$$

$$y = 44 - \frac{0.046 x}{0.22}$$

elastic special

Ek conserved

$$\frac{1}{2} m_c v_c^2 = \frac{1}{2} m_c y^2 + \frac{1}{2} m_b x^2$$

$$44^2 = y^2 + \frac{0.046}{0.22} x^2$$

$$0.046/0.22=0.2091$$

$$44^2 = 1,936 = (44 - 0.2091x)^2 + 0.2091x^2$$

$$44 \times 0.2091 = 9.2004 \quad 9.2004 \times 2 = 18.4008$$

$$0.2091 \times 0.2091 = 0.0437$$

$$1936 = 1936 - 18.4008x + 0.0437x^2 + 0.2091x^2$$

$$0 = -18.4008x + 0.0437x^2 + 0.2091x^2$$

$$0.2091 + 0.0437 = 0.2528$$

$$0 = -18.4008x + 0.2528x^2$$

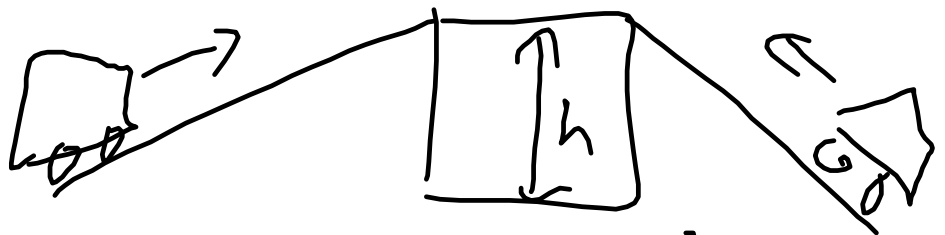
$$x = 18.4008 / 0.2528 = 72.788$$

$$y = 44 - (0.2091 \times 72.788) = 28.78$$

club moves at 28.8 m/s and the ball moves at 72.8 m/s

p212  
AC3

2.0m high platform  
3.0m ramp  
4.0m ramp



$$\Delta E_{\text{energy}} = W = mgh$$

$$F_k = 0$$

if there is no energy lost to frictional forces, the

work done is path independent =  $mgh$  using either ramp.

what if there is friction of 2.0N? then the shorter ramp would require less work.

the ramp doesn't make less work, it makes easier work - less force in this case.

### Problem 4 p213

$W$  = change in energy or  $F \times d$

$W = mgh$

density = mass / volume

so mass = density x volume

$m = 2000 \times 1.15 = 2300.0 \text{ kg}$

$F_g = 2300 \times 9.8 = 22540 \text{ N}$

$F_{\text{total}} = 22540 + 2250 = 24790 \text{ N}$

$W = F \times d = 24790 \times 7.5 = 185925 \text{ J}$

$W = 1.86 \times 10^5 \text{ J}$  or 186kJ

15 minutes:

work on p212-214 AC 1-7, Prob1,4,5,16,20  
p237-239 AC1,3,5,7,13 Prob 3,8,22,29,31

if you are done, study by doing all the other

problems

p213

AC 7

How do you increase the IMA, ideal mechanical advantage?

$IMA = d_{in} / d_{out}$

increase the  $d_{in}$  - the distance the input force acts

examples:

use a pulley with more ropes -

use a wrench and push on the outside

use a longer ramp

lower gear on your bike

p237

Problem 3c

a)  $E_k = 0.5 \times 45 \times 10^2 = 2,250 \text{ J}$

b)  $0.5 \times 45 \times 5^2 = 562.5 \text{ J}$

c)  $E_{ka} / E_{kb} = 2250 / 562.5 = 4$  times the kinetic energy with double the speed

kinetic energy is proportional to the velocity  
**squared**

p237 AC 13

pop ups in baseball, the second goes twice as high, how do their speeds compare?

$$mgh = \frac{1}{2}mv^2$$

$$gh = \frac{1}{2}v^2$$

$$v^2 = 2gh$$

$$v_1 = \sqrt{2gh}$$

$$v_2 = \sqrt{2g(2h)} = \sqrt{2} \times \sqrt{2gh} = \sqrt{2} \times v_1$$

$$v_2 = \sqrt{2} \times v_1$$

so the second popup is faster by a factor of the square root of 2 to get twice as high.

p238 Q8

$$W = Fxd = 5.00 \times 10^5 \text{N} \times 500 \text{m} = 2.5 \times 10^8 \text{J}$$

b) change in kinetic energy = Work done  
=  $2.5 \times 10^8 \text{J}$

c)  $2.5 \times 10^8 \text{J}$

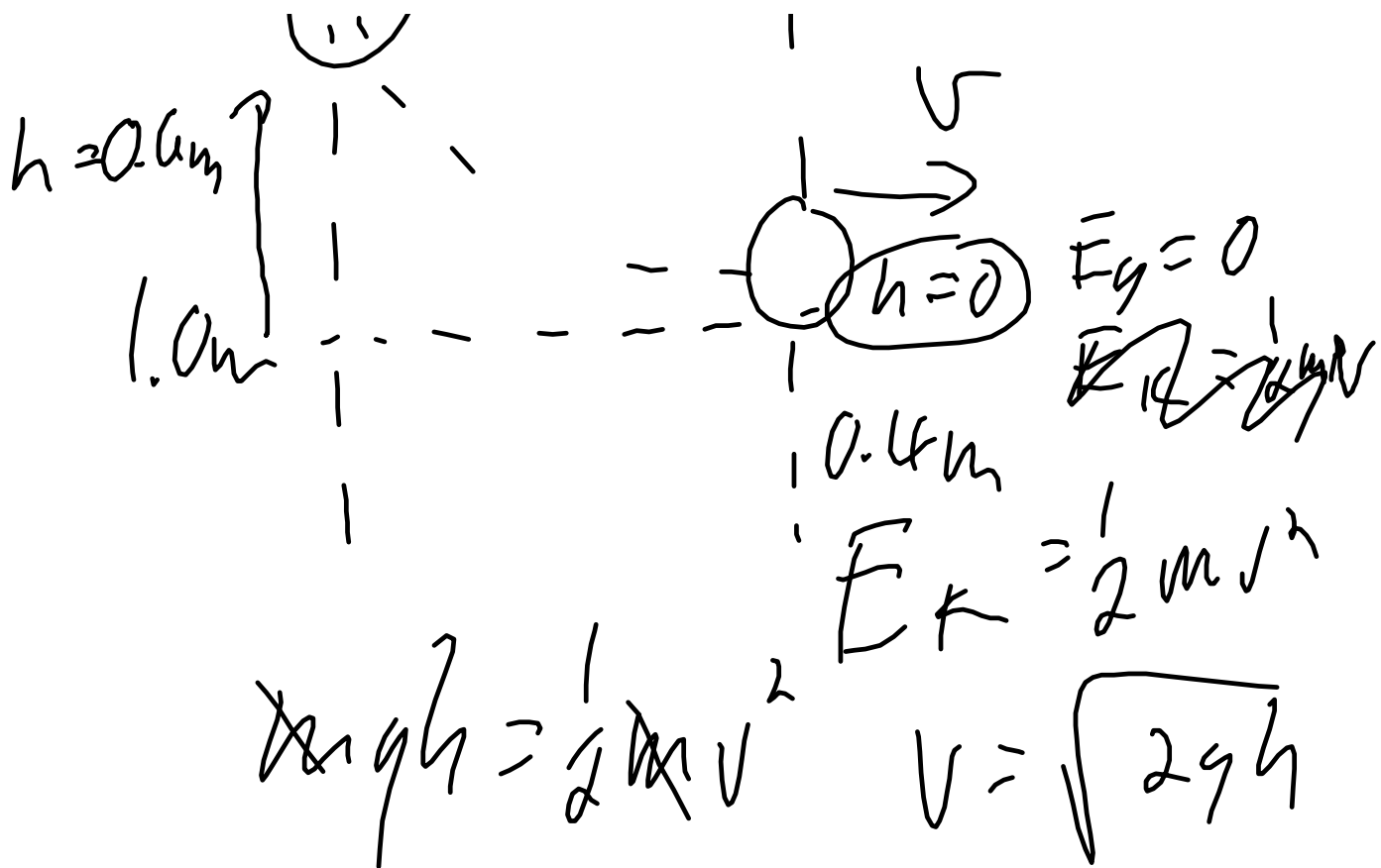
d)  $\frac{1}{2}mv^2 = \text{Energy}$

$$v = \sqrt{2 \times 2.5 \times 10^8 / 2.5 \times 10^4} = 141.4213562373095$$

141m/s

p239  
Q24





$$mgh = \frac{1}{2}mv^2 \quad v = \sqrt{2gh}$$

$$v = \sqrt{2 \times 9.8 \times 0.6}$$

$$b) E_k = \frac{1}{2}mv^2$$

$$\frac{1}{2} \left( \frac{420}{9.8} \right) (2)^2 = 85.7 \text{ J}$$

$\uparrow m = \frac{F_g}{g}$

$$mgh = 420 \times 0.6 = 252 \text{ J}$$

$$[-166 \text{ J } E_{\text{m}}]$$

15 minutes:

work on p212-214 AC 1-7, Prob1,4,5,16,20  
p237-239 AC1,3,5,7,13 Prob 3,8,22,29,31

if you are done, study by doing all the other problems

Q15 p235

superman hit by a bullet with a perfectly elastic collision - how do you determine the velocity of the bullet and superman after the collision.

collision or explosion - momentum is conserved

perfectly elastic collision - momentum and kinetic energy are conserved

2 equations with 2 unknowns and you sub in

$$m_1v_1 + m_2v_2 = m_1x + m_2y$$

$$\frac{1}{2} m_1v_1^2 + \frac{1}{2} m_2v_2^2 = \frac{1}{2} m_1x^2 + \frac{1}{2} m_2y^2$$

$$0.0042x835 + 0 = 0.0042x + 104y$$

$$x = 835 - (104/0.0042)y$$

$$104/0.0042 = 24,761.9048$$



$$104/0.0042=24,761.9048$$

$$1/2 \cdot 0.0042 \times 835^2 + 0 = 1/2 \cdot 0.0042 x^2 + 1/2 \cdot 104 y^2$$

$$835^2 = x^2 + 24761.9y^2$$

$$835^2 = (835 - 24761.9y)^2 + 24761.9y^2$$

$$835 \times 24761.9 = 2.0676E7 \quad 2.0676E7 \times 2 =$$

$$41,352,000 \quad 24761.9^2 = 6.1315E8$$

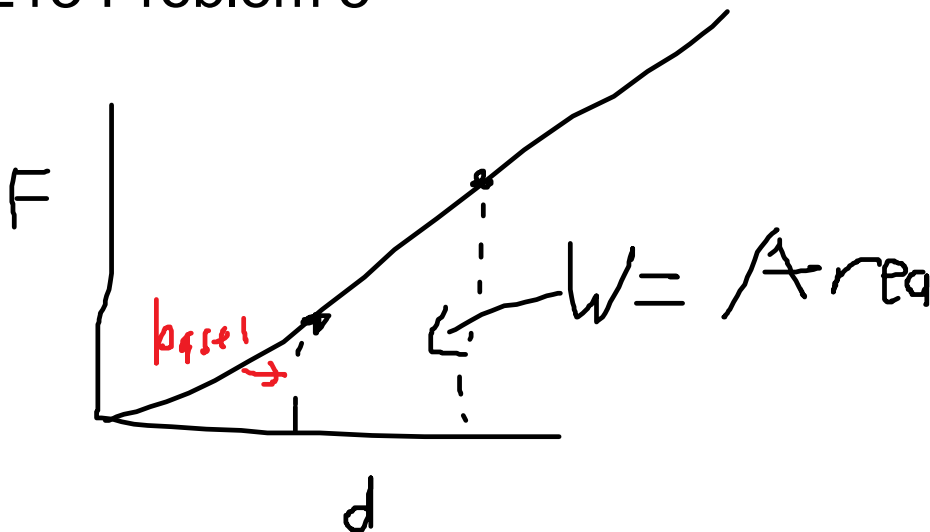
$$835^2 = 835^2 - 41352000y + 6.1315 \times 10^8 y^2 + 24761.9y^2$$

$$6.1315E8 + 24761.9 = 6.1317E8$$

$$0 = -41352000y + 6.1315 \times 10^8 y^2 + 24761.9y^2$$

$$y = 41352000 / 6.1317E8 = 0.0674 \text{ m/s}$$

p213 Problem 5



$$\text{Area} = 1/2 (\text{base1} + \text{base2})h$$

$$W = 0.5 \times (3+7) \times (0.28-0.12) = 0.80 \text{ J}$$

area under a F-d graph is work = change in energy

p238

Problem 8

$$\text{mass} = 2.50 \times 10^4 \text{kg}$$

$$F = 5.00 \times 10^5 \text{N}$$

$$d = 500 \text{m}$$

$$\text{a) } W = Fd = 500000 \times 500 = 250000000 \\ 2.50 \times 10^8 \text{J}$$

$$\text{b) } \Delta E_k = W = 2.50 \times 10^8 \text{J}$$

$$\text{c) if } E_{ki} = 0, \text{ the } E_{kf} = 2.50 \times 10^8 \text{J}$$

$$\text{d) } \frac{1}{2}mv^2 = E_k$$

$$v = \sqrt{(2E_k/m)} = \text{Sqrt}(2 \times 2.5 \text{E}8 / 2.5 \text{E}4) = \\ 141.4213562373095$$

$$141 \text{ m/s}$$